

# Genetic value of animal



## Modul no. 3: Animal Breeding

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# The importance and place of knowledge of the genetic value of animal in the process of animal breeding

- Breeding goals
  - Animal pedigrees (DNA tests, genotyping)
- **Genetic Value - Estimation of Breeding Values**
  - Selection and mating
  - Creating a new generation
    - Genetic gain



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# Genetic value of animal - concept

## Genetic value - estimation of breeding values

When estimating breeding values, we start from the knowledge that the overall phenotypic expression of any trait can be expressed according to the basic biological equation:

$$P = G + E$$

P - phenotype, G - genotype, E - environment



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# Genetic value of animal - concept

## Breeding value.

It represents an estimate of the genetic makeup (genetic value) of an individual for a specific trait .

It is most often expressed in the form of a deviation from the average of the population (group) of animals (absolute breeding values, relative breeding values).

The term breeding value is generally used to estimate genetic value for traits of a quantitative nature.

Individual breeding values form part of the simple or complex selection indices.



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# Estimation of breeding values - history - future

## Significant methods of estimating breeding values

Mother-daughter method  
CC (Contemporary Comparison) test

## The BLUP method

## *Genomic approaches in estimating breeding values*



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# Estimation of breeding values - BLUP method

**B**est **L**inear **U**nbiased **P**rediction

Linear model with mixed effects.

Simultaneous use of fixed and random effects.

Practical use even for unbalanced data sets.

Any number of environmental effects.

The method is based on mixed model theory for the simultaneous estimation of genetic and environmental effects, and is closely related to the method of estimating the components of variance in these models (Henderson, 1953, 1954).



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# Estimation of breeding values - BLUP method

## **BLUP - sire model** (Paternal model)

Estimation of breeding values of only some individuals in the population (usually males).

## **BLUP - animal model** (Individual model)

Estimation of the breeding values of all individuals in the population.

Use of all available information in the estimation: pedigree, own performance, descendants, other relatives in the collateral line.

Single-trait models

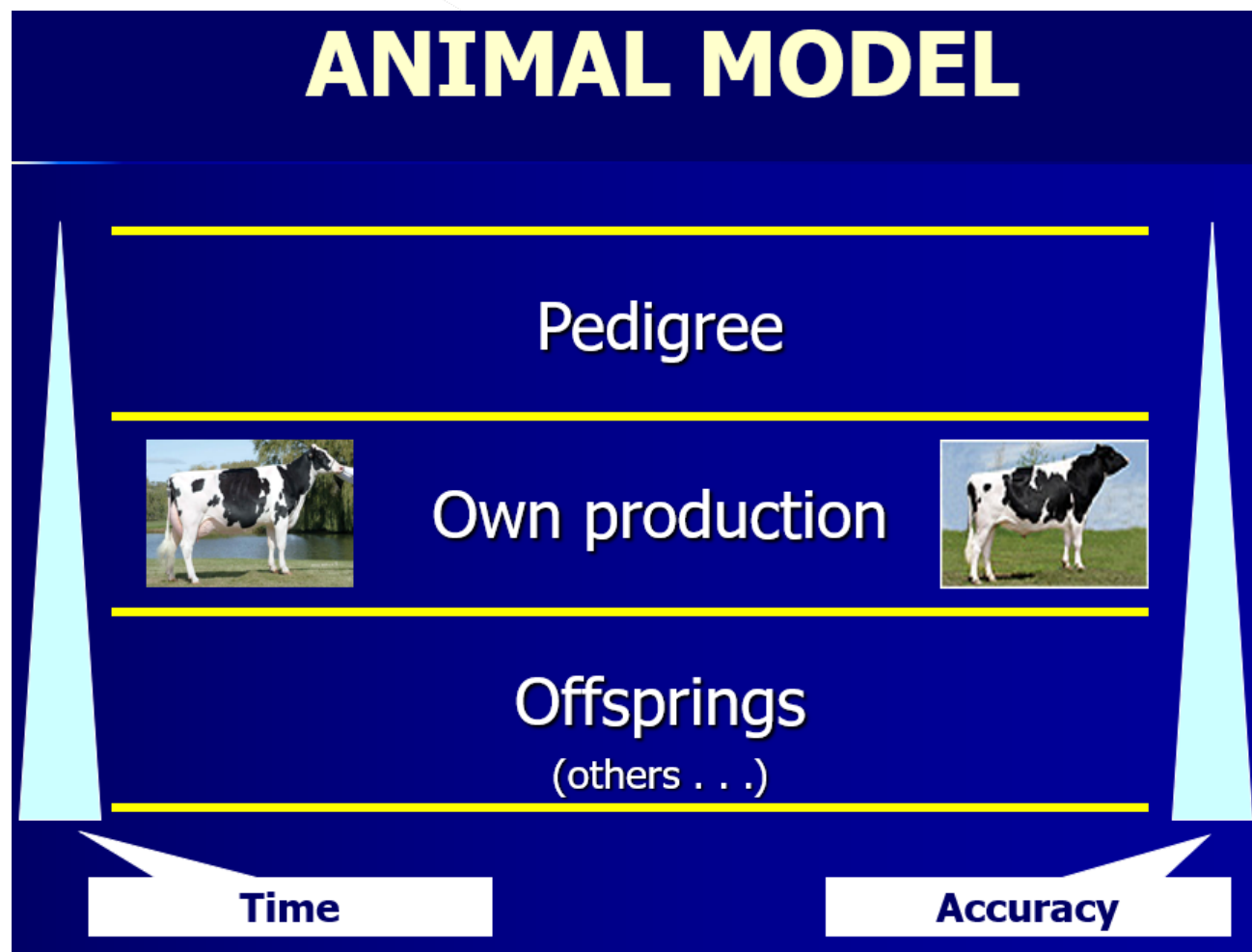
Multiple-traits models



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# Estimation of breeding values – BLUP animal model

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Source: Breeding value estimation, Candrák, 2007

# Estimation of breeding values – BLUP animal model

## BLUP - Animal model (without taking into account family relationships)

We can simply write the model schematically:

**y = average + environmental effects + animal + residue**

in matrix notation:

$$\mathbf{y} = \mathbf{Xb} + \mathbf{Za} + \mathbf{e}$$

y Column vector of phenotypic observations (measured utility)

b column vector of unknown fixed effects

a column vector of unknown random effects (breed values),  $N(0, )$

X, Z matrix of explanatory variables assigning utility to fixed and random effects

e random error vector (residual),  $N(0, )$



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# Estimation of breeding values – BLUP animal model

**BLUP - Animal model** (without taking into account family relationships)

Model solution:

$$\begin{bmatrix} X'X & X'Z \\ Z'X & Z'Z + Ik \end{bmatrix} \begin{bmatrix} b \\ a \end{bmatrix} = \begin{bmatrix} X'y \\ Z'y \end{bmatrix} \quad k = (1 - h^2)h^2$$

**BLUP - Animal model** (taking into account family relationships)

Model solution:

$$\begin{bmatrix} X'X & X'Z \\ Z'X & Z'Z + A^{-1}k \end{bmatrix} \begin{bmatrix} b \\ a \end{bmatrix} = \begin{bmatrix} X'y \\ Z'y \end{bmatrix}$$



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# Estimation of breeding values– BLUP animal model

**BLUP - Animal model** (Consideration of genomic information)

Model solution:

$$\begin{bmatrix} X'X & X'Z \\ Z'X & Z'Z + H^{-1}k \end{bmatrix} \begin{bmatrix} b \\ a \end{bmatrix} = \begin{bmatrix} X'y \\ Z'y \end{bmatrix}$$

The  $H^{-1}$  matrix is calculated according to the following relation:

$$H^{-1} = A^{-1} + \begin{bmatrix} 0 & 0 \\ 0 & G^{-1} - A_{22}^{-1} \end{bmatrix}$$

$G^{-1}$  is an inverse genomic matrix  $A_{22}^{-1}$  is the inverse matrix of the additive affinity of genotyped animals calculated on the basis of pedigree information.



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# Estimation of breeding values – BLUP animal model

**BLUP - Animal model** (model with maternal effects )

The model can be written as:

$$y = Xb + Z_1a + Z_2m + Z_3p + e,$$

y – the trait evaluated;  
a - additive genetic effect,  
m - maternal genetic effect,  
p - permanent effect of the environment,  
e - residue



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# Estimation of breeding values – nonlinear models

## Survival analysis

It is based on nonlinear regression analysis.

It allows you to take into account environmental influences and factors that are time-dependent and also evaluates censored data (it also processes incomplete information).

Survivability models are built on two features:  
**function and survival function.**

The hazard function measures the risk of discarding an animal at a certain time.

The survivability function expresses the probability of survival up to a certain period of time.



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# Thank you for your attention!

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